

WOMEN'S UNIVERSITY IN AFRICA



Addressing gender disparity and fostering equity in University Education

FACULTY OF MANAGEMENT AND ENTREPRENEURIAL SCIENCES

BSc HONOURS DEGREE IN COMPUTER SCIENCE

MAIN PAPER

HCS 112: MATHEMATICAL FOUNDATIONS OF COMPUTER SCIENCE

INTAKE 3: FIRST YEAR FIRST SEMESTER

TIME: 2 HOURS AFTERNOON

INSTRUCTIONS TO CANDIDATES

Answer any **four** questions.

Question 1

- a) Let $A = \begin{bmatrix} 2 & 1 & 4 \\ 3 & 5 & -7 \\ 1 & 6 & 2 \end{bmatrix}$
- Find the adjoint of the matrix A [5]
 - Hence or otherwise find inverse of matrix A [5]
- b) Let $p = 2\mathbf{i} - 3\mathbf{j} + 4\mathbf{k}$ and $q = \mathbf{i} + 2\mathbf{j} + \mathbf{k}$, show that the vectors p and q are orthogonal [4]
- c) State De Moivre 's Formula [4]
- d) Show that $\cos 5\theta = 16 \cos^5\theta - 20\cos^3\theta + 5 \cos\theta$ [7]

Question 2

- a) Solve:
- $5x^2 + 2x + 2 = 0$ [3]
 - $x^3 - 7x^2 + 17x - 15 = 0$ [5]
- b) Find the vector equation of the straight line which passes through the points (1, 2, 3) and is parallel to the straight line through the points (-1, 2, 7) and (2, 3, 4) [6]
- c) Let $p = 2\mathbf{i} + 3\mathbf{j} - \mathbf{k}$ and $q = \mathbf{i} - 4\mathbf{j} + 5\mathbf{k}$. Find $p \cdot q$ and the angle between them [4]
- d) Find $(2 + 3\mathbf{i})(1 + 2\mathbf{i})$ [2]
- e) Prove that if an $n \times n$ matrix A is multiplied by a scalar k, then the determinant of kA is $k^n \det A$ [5]

Question 3

- a) If $z_1 = r_1 (\cos \alpha_1 + \mathbf{i} \sin \alpha_1)$ and $z_2 = r_2 (\cos \alpha_2 + \mathbf{i} \sin \alpha_2)$
Prove that $z_1 z_2 = r_1 r_2 (\cos(\alpha_1 + \alpha_2) + \mathbf{i} \sin(\alpha_1 + \alpha_2))$ [9]
- b) Show that $\cos^3 \alpha = \frac{1}{4} \cos 3\alpha + \frac{3}{4} \cos \alpha$ [9]
- c) Find the square root of $8 - 6\mathbf{i}$ [7]

Question 4

a) Find the solution of the linear system using Cramer's rule

$$x_1 + 2x_2 + 4x_3 = 14$$

$$2x_1 + 6x_2 + 6x_3 = 28$$

$$3x_1 + 6x_2 + 10x_3 = 34 \quad [13]$$

b) Prove that if the determinant of an $n \times n$ matrix A is 0, then the matrix does not have an inverse [12]

Question 5

a) Find A^{-1} if $A = \begin{bmatrix} 1 & -2 & 4 \\ -4 & 0 & 3 \\ 2 & -1 & 0 \end{bmatrix}$ [6]

b) A straight line passes through the points $(2, 1, 7)$ and $(-3, 2, 5)$. Find

i. Parametric equations of the line [3]

ii. Symmetric equation of the line [4]

c) Show that $\sin 4\theta = \frac{1}{4} \cos 4\theta - \cos 2\theta + \frac{3}{4}$ using Euler's formula [12]

Question 6

Solve the system of equations

a) $2x_1 + 3x_2 - x_3 = 4$

$$x_1 - 2x_2 + x_3 = 6$$

$$x_1 - 12x_2 + 5x_3 = -10 \quad [15]$$

b) Convert each of the following complex numbers to a polar form

$$2\sqrt{3} + 2i \quad [5]$$

c) Let $R = \begin{bmatrix} 3 & 4 & 1 \\ 0 & 2 & -6 \\ 8 & 5 & 7 \end{bmatrix}$ and $R^t = \begin{bmatrix} 3 & 0 & 8 \\ 4 & 2 & 5 \\ 1 & -6 & 7 \end{bmatrix}$ find $R - R^t$ and name the special name

given to this matrix [5]

END